

(8) : Given, radius of curvature, $R = 2\text{m}$

Focal length of mirror, $f = \frac{R}{2} = 1\text{ m}$

Distance of approaching car = 24 m

From mirror formula $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$$\text{or } v = \frac{u \cdot f}{u - f} = \frac{(-24) \cdot (1)}{(-24 - 1)} = \frac{24}{25}$$

$$\text{Magnification, } m = \frac{-v}{u} = \frac{-24}{25 \times (-24)} = \frac{1}{25} \quad \dots(i)$$

From lens formula $\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$

Speed of image, $v_I = m^2 v_o$, where v_o is speed of object

$$= \frac{-1}{(25)^2} (25)$$

$$v_I = \frac{-1}{25} \quad \dots(ii)$$

Differentiating the lens formula, $\frac{-1}{v^2} \frac{dv}{dt} + \frac{1}{u^2} \frac{du}{dt} = 0$

Differentiating it again with respect to time.

$$\frac{2}{v^3} \left(\frac{dv}{dt} \right)^2 - \frac{1}{v^2} \left(\frac{d^2v}{dt^2} \right) - \frac{2}{u^3} \left(\frac{du}{dt} \right)^2 + \frac{1}{u^2} \frac{d^2u}{dt^2} = 0$$

$$\frac{2}{v^3} (v_I)^2 - \frac{1}{v^2} (a) - \frac{2}{u^3} (v_o)^2 + \frac{a_o}{u^2} = 0$$

Since, $a_o = 0$

$$\therefore a = 2v^2 \left(\frac{v_I^2}{v^3} - \frac{v_o^2}{u^3} \right)$$

$$a = \frac{(2)(25)}{24} \cdot \left(\frac{-1}{25} \right)^2 - \frac{2}{(24)^3} \left(\frac{24}{25} \right)^2 \cdot (25)^2$$

$$a = \frac{1}{(12)(25)} - \frac{1}{12} = \frac{1}{12} \left[\frac{1}{25} - \frac{1}{1} \right]; \quad a = \frac{-2}{25}$$

$$\therefore |100a| = \frac{2}{25} \times 100 = 8$$